

# Calculation of height of clouds observed 19/2-2013 from Copenhagen. by Tom Axelsen

What is known!

Sunset Copenhagen (CPH) : 17:24 CET

Sunset at clouds as seen

from CPH : 18:20 CET

Direction to sun as seen

from CPH at 18:20 CET

Altitude :  $-8^\circ$

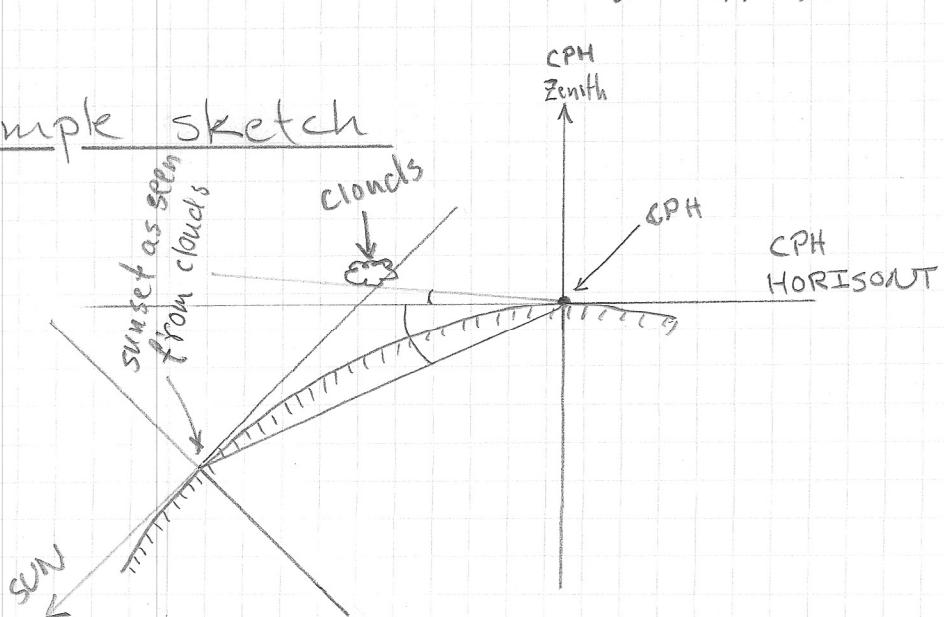
Azimuth :  $262^\circ$

Direction to clouds from CPH at 18:20 CET

Altitude : app.  $8^\circ$  (center of clouds)

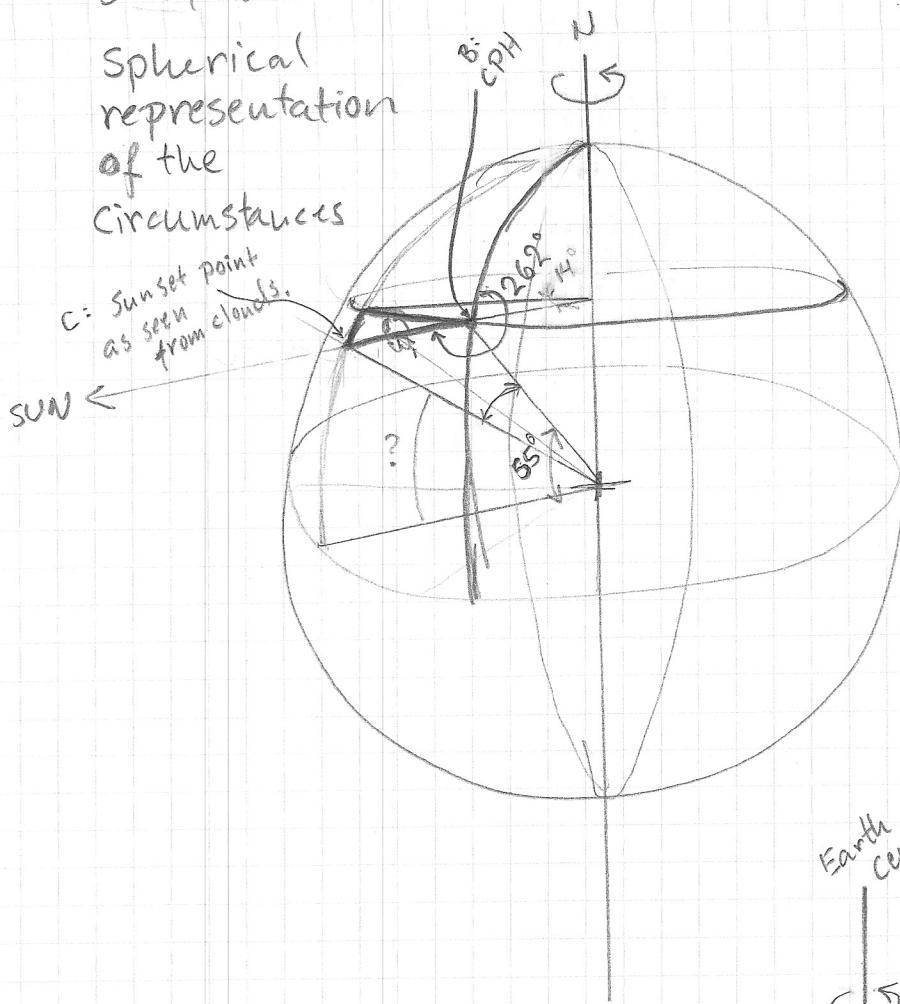
Azimuth :  $262^\circ$  (brightest part of clouds)  
in sun direction

## Simple sketch



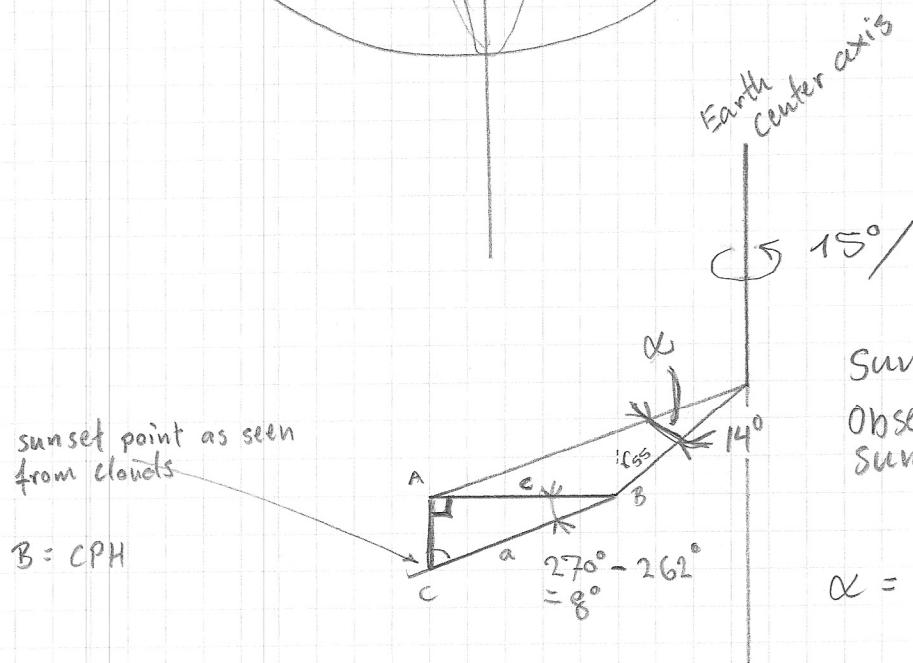
### Sketch with

spherical representation  
of the  
circumstances



**IMPORTANT NOTE!**  
None of the angles or  
lengths shown in the  
sketches are to scale!

The purpose of the  
sketches is to keep track  
of what length or  
angle I am  
calculating!



Sunset CPH 17:24

Observed  
Sunset clouds 18:20

$$(18:20 - 17:24)$$

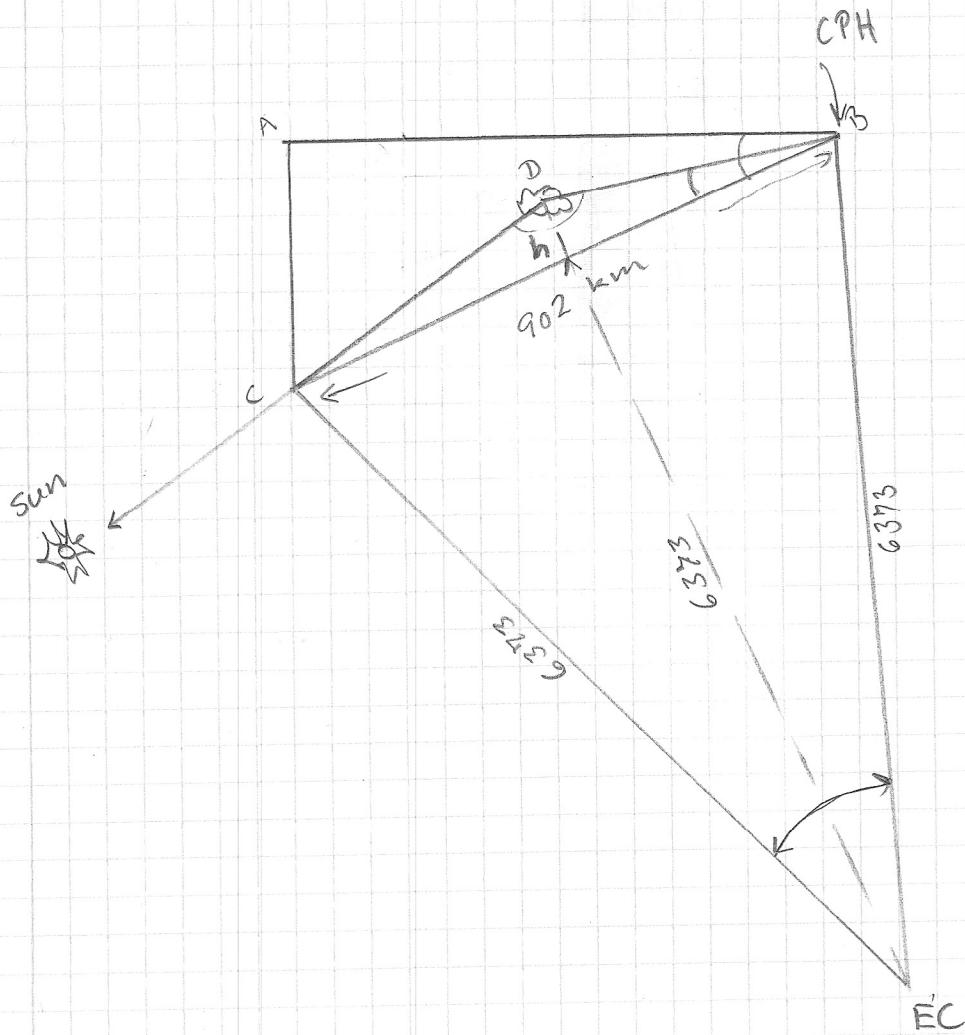
$$\alpha = \frac{56 \text{ m}}{60 \text{ m/h}} \times 15^\circ/\text{h}$$

$$= 14^\circ$$

$$r_{55} = 3655 \text{ km}$$

$$c = 3655 \times 2\pi \cdot \frac{14}{360} = 893 \text{ km}$$

$$a \sim \frac{893}{\cos(14^\circ)} = 902 \text{ km}$$

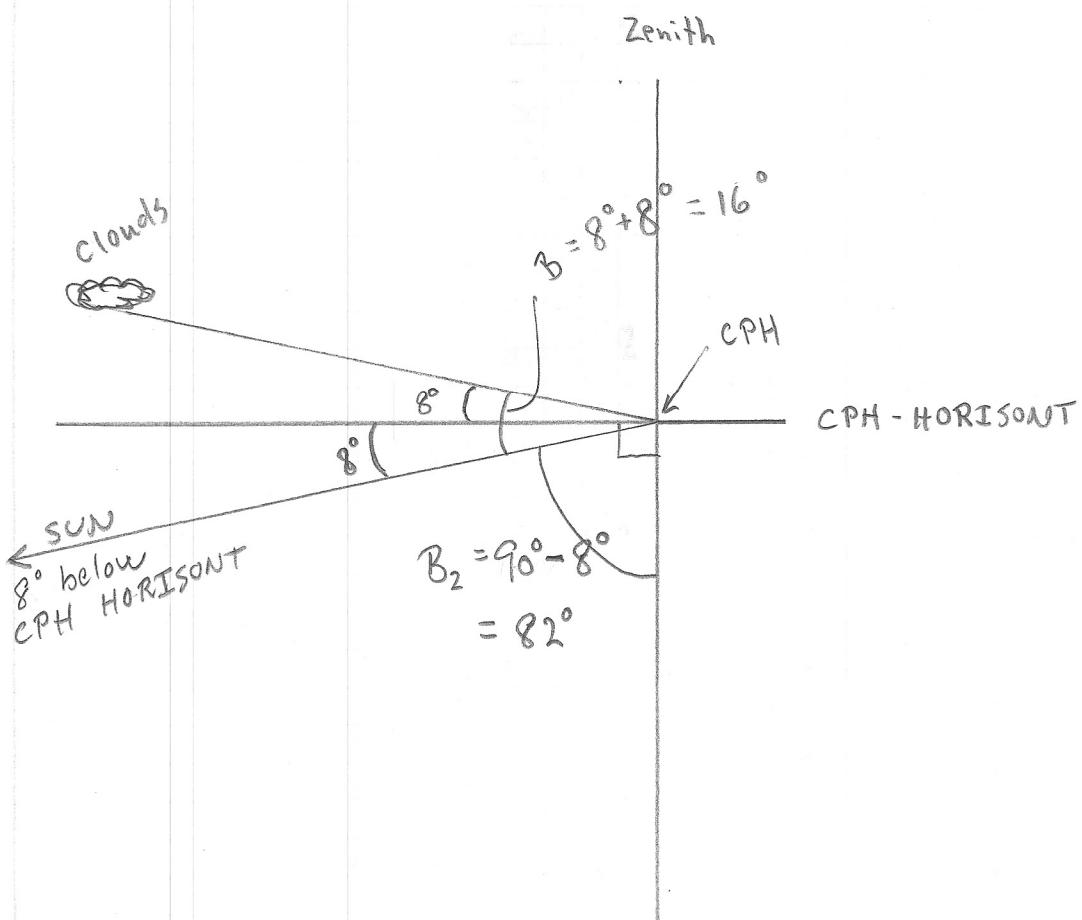


$$EC = \frac{902 \text{ km}}{6373 \times 2\pi} \times 360^\circ = 8,1^\circ$$

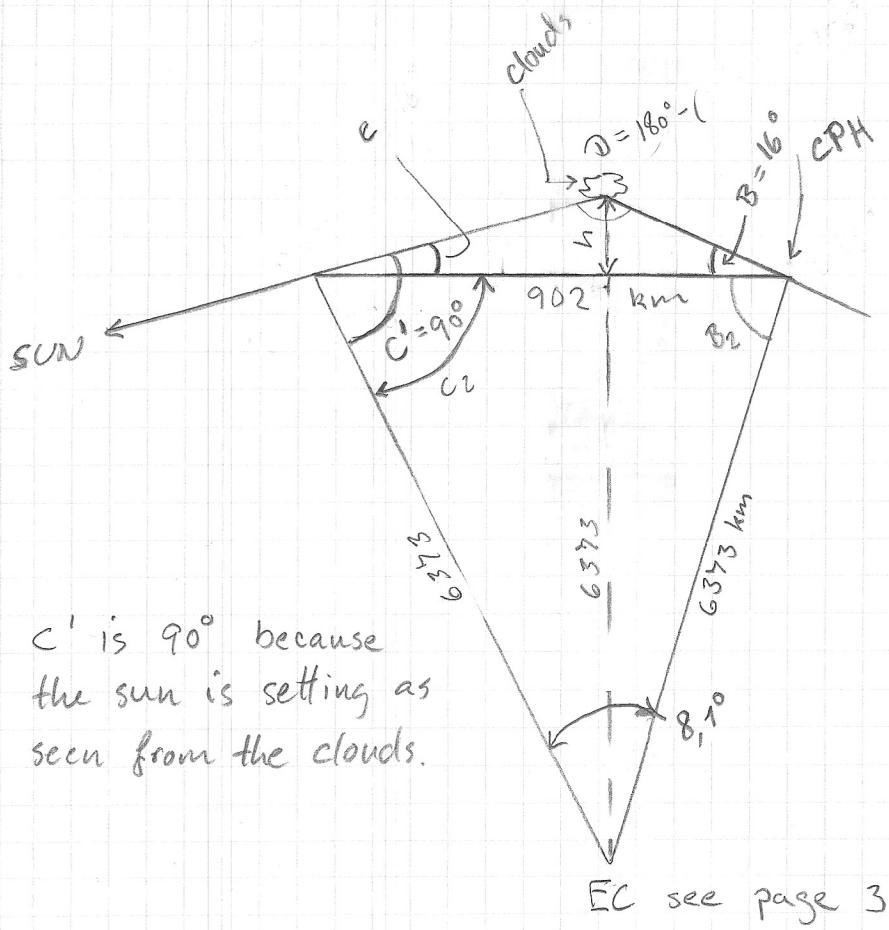
EC is the angle as seen from Earth Center between the two points on Earths surface.

Observing site : CPH

sunset point as seen from the clouds : C



Calculation of  $B$  and  $B_2$



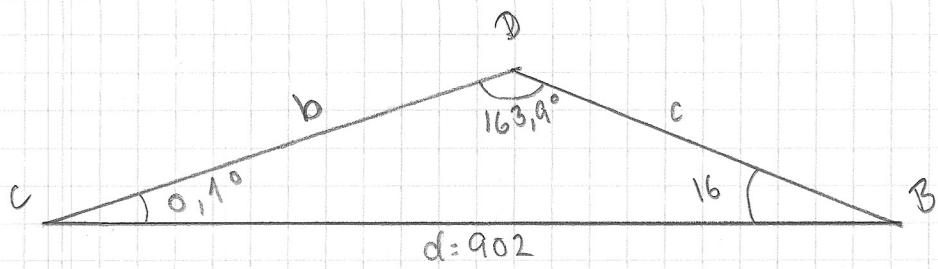
$$B = 16^\circ$$

$$B_2 = 82^\circ \quad \text{see page 4.}$$

$$C_2 = 180^\circ - (B_2 + EC) = 89,9^\circ$$

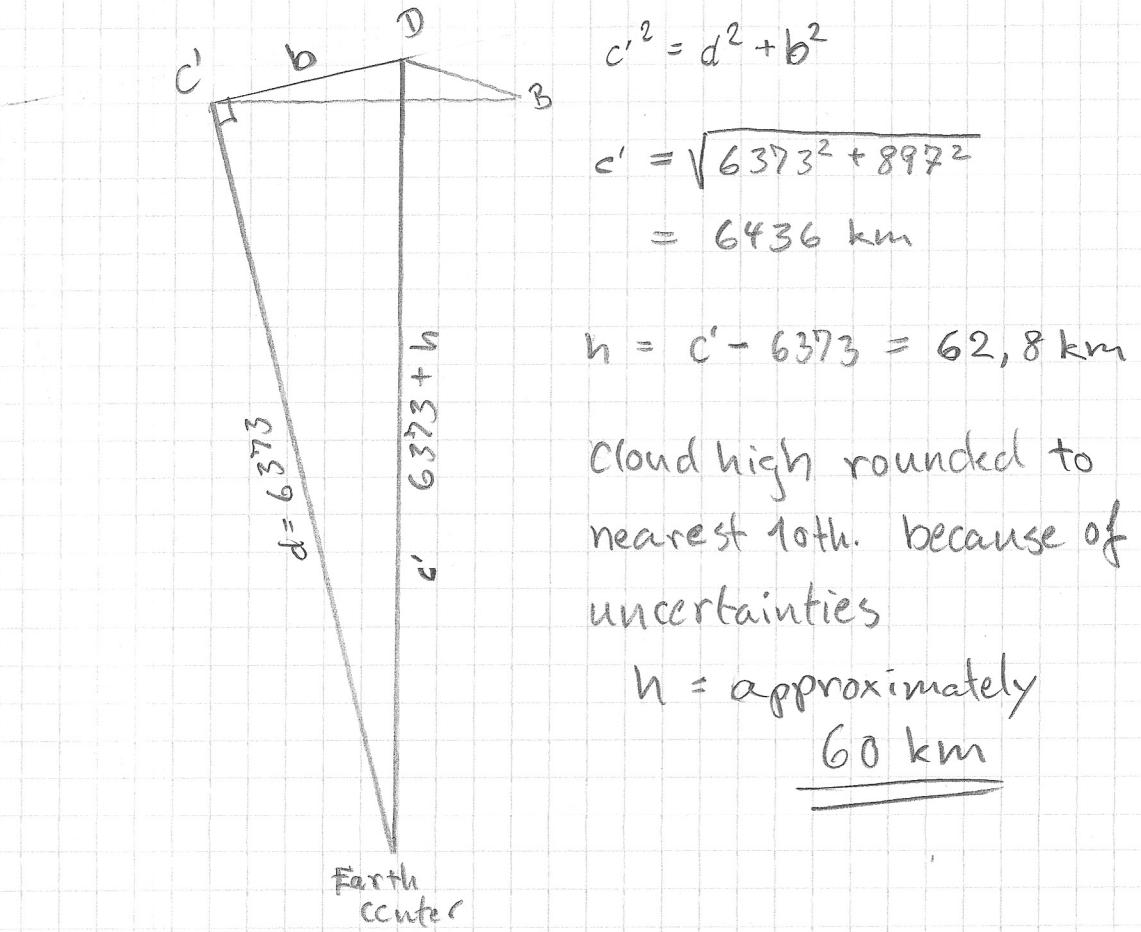
$$C = 90 - 89,9^\circ = 0,1^\circ$$

$$D = 180^\circ - (B + C) = 163,9^\circ$$



$$\frac{b}{\sin(B)} = \frac{d}{\sin(D)}$$

$$b = \frac{902 \times \sin(16^\circ)}{\sin(163,9^\circ)} = 897 \text{ km}$$



$$\begin{aligned} c'^2 &= d^2 + b^2 \\ c' &= \sqrt{6373^2 + 897^2} \\ &= 6436 \text{ km} \end{aligned}$$

$$h = c' - 6373 = 62,8 \text{ km}$$

Cloud high rounded to nearest 10th. because of uncertainties

$$h = \underline{\text{approximately}} \underline{60 \text{ km}}$$